

91

$$\lim_{x \rightarrow +\infty} \frac{\log(3^x + x^2 - 5x + 2 \arctan x)}{\log(3^{5x} + x^4 + 2x^2 - 3)} =$$

$$= \lim_{x \rightarrow +\infty} \frac{\log 3^x + \log\left(1 + \frac{x^2}{3^x} - \frac{5x}{3^x} + \frac{2 \arctan x}{3^x}\right)}{5 \log 3^x + \log\left(1 + \frac{x^4}{3^{5x}} + \frac{2x^2}{3^{5x}} - \frac{3}{3^{5x}}\right)}$$

$$= \lim_{x \rightarrow +\infty} \frac{1 + \frac{\log\left(1 + \frac{x^2}{3^x} - \frac{5x}{3^x} + \frac{2 \arctan x}{3^x}\right)}{\log 3^x}}{5}$$

$$= \lim_{x \rightarrow +\infty} \frac{1 + \frac{\log\left(1 + \frac{x^4}{3^{5x}} + \frac{2x^2}{3^{5x}} - \frac{3}{3^{5x}}\right)}{5 \log 3^x}}{5}$$

=  $\frac{1}{5}$