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$$\lim_{x \rightarrow +\infty} \frac{\log(3^{2x} + 1) + \sqrt{\log(e^x + 2)}}{3x + 1 + \sqrt{x} \arctan x} =$$

$$= \lim_{x \rightarrow +\infty} \frac{\log 3^{2x} + \log\left(1 + \frac{1}{3^{2x}}\right) + \sqrt{x + \log\left(1 + \frac{2}{e^x}\right)}}{x \left(3 + \frac{1}{x} + \frac{\arctan x}{\sqrt{x}}\right)} =$$

$$= \lim_{x \rightarrow +\infty} \frac{2 \log 3^x + \log\left(1 + \frac{1}{3^{2x}}\right) + \sqrt{x} \sqrt{1 + \frac{\log(1 + 2/e^x)}{x}}}{x \left(3 + \frac{1}{x} + \frac{\arctan x}{\sqrt{x}}\right)} =$$

$$= \lim_{x \rightarrow +\infty} \frac{2 \log_3 3^x \cdot \log e}{x \left(3 + \frac{1}{x} + \frac{\arctan x}{\sqrt{x}}\right)}$$

$$= \lim_{x \rightarrow +\infty} \frac{2 \log_3 3^x \cdot \log e}{x \left(3 + \frac{1}{x} + \frac{\arctan x}{\sqrt{x}}\right)}$$

$$\log 3^x = \log_3 3^x \cdot \frac{1}{\log_3 e} = \log_3 3^x \log 3$$

$$= \lim_{x \rightarrow +\infty} \frac{2x \log 3 + \log\left(1 + \frac{1}{3^{2x}}\right) + \sqrt{x} \sqrt{1 + \frac{\log(1 + 2/e^x)}{x}}}{x \left(3 + \frac{1}{x} + \frac{\arctan x}{\sqrt{x}}\right)}$$

$$= \lim_{x \rightarrow +\infty} \frac{2 \log 3 + \frac{\log\left(1 + \frac{1}{3^{2x}}\right)}{x} + \frac{1}{\sqrt{x}} \sqrt{1 + \frac{\log(1 + 2/e^x)}{x}}}{3 + \frac{1}{x} + \frac{\arctan x}{\sqrt{x}}}$$

$$= \frac{2}{3} \log 3$$