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$$\lim_{x \rightarrow 2} \left(\sqrt[5]{3^x + x - 20} - 1 \right) \text{ by } \text{L'Hôpital's rule}$$

$$y = x - 2$$

$$x = y + 2$$

$$\lim_{y \rightarrow 0} \left(\sqrt[5]{3^{y+2} + y + 2 - 11 + 1} - 1 \right) \text{ by } \text{L'Hôpital's rule} =$$

$$= \lim_{y \rightarrow 0} \left(\sqrt[5]{3^{y+2} + y - 8} + 1 - 1 \right)$$

$$\lim_{y \rightarrow 0} \left(\frac{\sqrt[5]{(3^{y+2} + y - 9) + 1} - 1}{3^{y+2} + y - 9} \right) (3^{y+2} + y - 9) \log \frac{\sec \pi y}{\pi y} \cdot \pi y =$$

$$= 0 + \lim_{y \rightarrow 0} \frac{1}{5} \lim_{y \rightarrow 0} (3^{y+2} + y - 9) \log \pi y =$$

$$= \frac{1}{5} \lim_{y \rightarrow 0} \left(\frac{3^{y+2} + 1}{y} \right) \cdot y \cdot \log \pi y$$

$$= \frac{1}{5} \lim_{y \rightarrow 0} \left(\frac{3^{y+2} - 9}{y} + 1 \right) y \log \pi y$$

$$= \frac{1}{5} \lim_{y \rightarrow 0} \left(\frac{9}{\pi} \frac{3^y - 1}{y} \cdot \pi y \log \pi y + \frac{1}{\pi} \cdot \pi y \log \pi y \right) =$$

$$= \frac{1}{5} \left(\frac{9}{\pi} \log 3 \cdot 0 + \frac{1}{\pi} \cdot 0 \right) = 0$$