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$$\lim_{x \rightarrow +\infty} \sqrt[4]{x^4 + 3x^3 + x^2 - x + 2} - x =$$

$$= \lim_{x \rightarrow +\infty} \frac{\sqrt{x^4 + 3x^3 + x^2 - x + 2} - x^2}{\sqrt[4]{x^4 + 3x^3 + x^2 - x + 2} + x}$$

$$= \lim_{x \rightarrow +\infty} \frac{\sqrt[4]{x^4 + 3x^3 + x^2 - x + 2} - x^2}{\left(\sqrt[4]{x^4 + 3x^3 + x^2 - x + 2} + x\right) \left(\sqrt{x^4 + 3x^3 + x^2 - x + 2} + x^2\right)^{-1}}$$

$$= \frac{x^3 \left(3 + \frac{1}{x} - \frac{1}{x^2} + \frac{2}{x^3}\right)}{x \left(\sqrt[4]{1 + \frac{3}{x} + \frac{1}{x^2} - \frac{1}{x^3} + \frac{2}{x^4}} + 1\right) x^2 \left(\sqrt{1 + \frac{3}{x} + \frac{1}{x^2} - \frac{1}{x^3} + \frac{2}{x^4}} + 1\right)}$$

$$= \frac{3}{2 \cdot 2} = \frac{3}{4}$$