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$$\lim_{x \rightarrow +\infty} e^{\frac{1}{x}} \sqrt{x^2 + x + 1} - \sqrt{x^2 + 2x + 5} =$$

$$= \lim_{x \rightarrow +\infty} e^{\frac{1}{x}} \sqrt{x^2 + x + 1} - \sqrt{x^2 + x + 1} + \sqrt{x^2 + x + 1} - \sqrt{x^2 + 2x + 5}$$

$$= \lim_{x \rightarrow +\infty} \sqrt{x^2 + x + 1} (e^{\frac{1}{x}} - 1) + \sqrt{x^2 + x + 1} - \sqrt{x^2 + 2x + 5} =$$

$$= \lim_{x \rightarrow +\infty} \frac{\sqrt{x^2 + x + 1}}{x} \frac{e^{\frac{1}{x}} - 1}{\frac{1}{x}} + \frac{x^2 + x + 1 - x^2 - 2x - 5}{\sqrt{x^2 + x + 1} + \sqrt{x^2 + 2x + 5}}$$

$$= 1 + \lim_{x \rightarrow +\infty} \frac{-x - 4}{x \left(\sqrt{1 + \frac{1}{x} + \frac{1}{x^2}} + \sqrt{1 + \frac{2}{x} + \frac{5}{x^2}} \right)} = \frac{1}{2} - \frac{1}{2} = 0$$