

(199)

$$\lim_{x \rightarrow +\infty} \left( \sin \frac{2}{x} \right)^{\pi - 2 \operatorname{arctg} x} = \phi \cdot \phi$$

$$= \lim_{x \rightarrow +\infty} (\pi - 2 \operatorname{arctg} x) \cdot \log \sin \frac{2}{x}$$

$$= \lim_{x \rightarrow +\infty} e^{\dots}$$

$$= \lim_{x \rightarrow +\infty} e^{(\pi - 2 \operatorname{arctg} x) \cdot \frac{\log \sin \frac{2}{x}}{\sin \frac{2}{x}}}$$

$$= \lim_{x \rightarrow +\infty} e^{\frac{\pi - 2 \operatorname{arctg} x}{\frac{2}{x}} \cdot \left( \sin \frac{2}{x} \cdot \log \sin \frac{2}{x} \right)}$$

$$= \lim_{x \rightarrow +\infty} e^{\dots}$$

$$= \lim_{x \rightarrow +\infty} e^{\frac{(\pi - 2 \operatorname{arctg} x) \cdot \frac{2}{x}}{\frac{2}{x}} \cdot \left( \sin \frac{2}{x} \cdot \log \sin \frac{2}{x} \right)}$$

$$= \lim_{x \rightarrow +\infty} e^{\dots}$$

$$= e^{-1 \cdot 1 \cdot 0} = e^0 = 1$$

verallgemeinern

$$\frac{\pi - 2 \operatorname{arctg} x}{\frac{2}{x}}$$

$$y = \pi - 2 \operatorname{arctg} x$$

$$x = \operatorname{tg} \frac{\pi + y}{2} = \frac{\operatorname{sen} \left( \frac{\pi + y}{2} \right)}{\cos \left( \frac{y + \pi}{2} \right)} = - \frac{1}{\operatorname{tg} \frac{y}{2}}$$

$$= \frac{y}{-\frac{2}{1} \operatorname{tg} \frac{y}{2}} = - \frac{y}{2 \operatorname{tg} \frac{y}{2}} = \frac{1}{-\operatorname{tg} \frac{y}{2}}$$

$$\lim_{x \rightarrow +\infty} \frac{\pi - 2 \operatorname{arctg} x}{\frac{2}{x}} = \lim_{y \rightarrow 0} \frac{1}{-\frac{\operatorname{tg} \frac{y}{2}}{\frac{y}{2}}} = -1$$