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$$\lim_{x \rightarrow \infty} \left(\frac{3^x + 6^x}{2^x + 3^x} \right)^{\frac{1}{\arctan x}}$$
$$= \frac{3^x + 6^x}{2^x + 3^x}$$

$$= \lim_{x \rightarrow \infty} e$$

$$\frac{1}{\arctan x} \log \left[1 + \left(\frac{3^x + 6^x}{2^x + 3^x} - 1 \right) \right]$$

$$= \lim_{x \rightarrow \infty} \frac{1}{\arctan x} \left(\frac{3^x + 6^x}{2^x + 3^x} - 1 \right) \log \left[1 + \frac{\left(\frac{3^x + 6^x}{2^x + 3^x} - 1 \right)}{\left(\frac{3^x + 6^x}{2^x + 3^x} - 1 \right)} \right] =$$

$$= \lim_{x \rightarrow \infty} \frac{x}{\arctan x} \cdot \frac{1}{2^x + 3^x} \left(3^x + 6^x - 2^x - 3^x \right) \cdot \log$$

$$= \lim_{x \rightarrow \infty} \frac{x}{\arctan x} \cdot \frac{1}{2^x + 3^x} \left(\frac{3^x - 1 + 6^x - 1}{x} - \frac{2^x - 1}{x} - \frac{2^x - 1}{x} \right)$$

$$= \lim_{x \rightarrow \infty} e \cdot 1 \cdot \frac{1}{2} \left(\log \frac{3 \cdot 6}{2 \cdot 3} \right) \cdot 1 =$$
$$= e$$

~~1. Puccini - Turandot / Tosca - 3 canotte~~

~~4. Prokofiev - Pietro e il lupo - The Chamber Orchestra of Europe - Claudio Abbado
CD + audio cassette~~

~~6. Prokofiev - Romeo & Giulietta (extract) - Berlin
Philharmoniker - Edo. Peters Salonen~~

$$\left[\frac{1 + \left(\frac{3^x + 6^x}{2^x + 3^x} - 1 \right)}{\left(\frac{3^x + 6^x}{2^x + 3^x} - 1 \right)} \right]^{\frac{3^x - 1}{x}}$$

$$= e \cdot \log \sqrt{3} = \sqrt{3}$$