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$$\lim_{x \rightarrow 0} \frac{1}{x} \left(e^x \sqrt{x^2+x+1} - \frac{\sqrt{5x^2+2x+1}}{1+x} \right) =$$

$$= \lim_{x \rightarrow 0} \frac{e^x(1+x)\sqrt{x^2+x+1} - \sqrt{5x^2+2x+1}}{x(1+x)}$$

$$= \lim_{x \rightarrow 0} \frac{[e^x(1+x)\sqrt{x^2+x+1} - \sqrt{5x^2+2x+1}]}{x(1+x)[e^x(1+x)\sqrt{x^2+x+1} + \sqrt{5x^2+2x+1}]}$$

$$\rightarrow \frac{(1+0)[e^0(1+0)\sqrt{0+0+1}]}{x}$$

$$= \frac{1}{2} \lim_{x \rightarrow 0} \frac{e^{2x}(1+x)^2(x^2+x+1) - 5x^2 - 2x - 1}{x}$$

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$$= \frac{[e^{x(1+x)}\sqrt{x^2+x+1} + \sqrt{5x^2+2x+1}]}{x(1+x)[e^{x(1+x)}\sqrt{x^2+x+1} - \sqrt{5x^2+2x+1}]} =$$

$$= \frac{1}{1(1+0)} = 1$$